

Fig. 5 Effect of Reynolds number on skin friction, $M_\infty = 1.42$.

calculations also illustrate these trends and indicate that the flow is separated for the lowest Reynolds number. Again, separation could not be confirmed with either the c_f or the flow direction data.

Conclusions

The results of the present investigation illustrate the sensitivity of the normal shock-wave/turbulent boundary-layer interaction to variations in Mach and Reynolds number for this flow. The Wilcox-Rubesin turbulence model provides a good representation of these effects for both the wall pressure and skin friction.

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J80-196 Downwash Impingement

B. N. Pamadi*
Indian Institute of Technology, Bombay, India

Introduction

WHEN operating over unprepared terrain, VTOL configurations are known to raise appreciable dust and

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*Assistant Professor, Dept. of Aeronautical Engineering.

debris. This not only results in loss of visibility for the pilot but also structural damage to propeller or engine compressor blading when they are hit by the sand particles or gravel lifted from the ground by the downwash impingement (Fig. 1).

Kuhn's studies¹ have shown that the bulk of the erosion or entrainment occurs close to the stagnation point and is confined to a region where the local surface dynamic pressure ($\frac{1}{2}\rho U^2$) exceeds a critical value. For dry sand and loose dirt, he finds that the critical surface dynamic pressure ranges 50-150 N/m². The dynamic pressure on the surface rises from zero at the stagnation point to a peak ($\frac{1}{2}\rho U_m^2$) at a point where the static pressure gradient vanishes and then starts falling off due to viscous decay (Fig. 1a). The conditions for incipient erosion are thus determined at the location of peak surface dynamic pressure. Kuhn's observations also reveal that the larger particles are predominantly rolled along the surface while the smaller ones are lifted from the ground.

The sand or dirt particles which are entrained are initially immersed in the boundary layer of the ground. The rolling of the particles occurs when the aerodynamic drag D exceeds the frictional force μW (drag entrainment) and the raising from the ground occurs if the aerodynamic lift L exceeds the particle weight W (lift entrainment). The particles develop lift because they are subjected to shear flow in the boundary layer.

For downwash flow with a uniform velocity distribution, Vidal² has developed some criteria for predicting lift and drag entrainment. His results are based upon the classical stagnation point boundary layer solution,³ applicable to a uniform impinging flow of infinite extent. However, the downwash flow on leaving the jet nozzle has spread and decay characteristics similar to those of a free turbulent jet. In view of this, Vidal's analysis is restricted to low operating heights where the jet mixing effects are small and the velocity is nearly uniform (potential core). The experimental investigations of free jet impingement on normal surface also show that the classical stagnation point solution is applicable only to a small region around the stagnation point.^{4,5} Reference 6 reports a more accurate solution for the ground boundary layer in the jet impingement region. Based upon this solution, Vidal's entrainment criteria are extended and presented here in a form applicable for any operating height above the ground surface. These results are in reasonably good agreement with Kuhn's experimental findings.

Criteria for Particle Entrainment

Vidal has given the following criteria,

Drag entrainment:

$$\frac{\rho_s g \delta_0}{\frac{1}{2}\rho U^2} \leq \frac{3}{2\sqrt{2}} C_D \left(\frac{u_0}{U}\right)^2 \left(\frac{\delta_0}{a}\right) \quad (1)$$

where $D/W \geq \mu$, $\mu = 1/\sqrt{2}$, and $C_D = 0.5$.

Lift entrainment:

$$\frac{\rho_s g \delta_0}{\frac{1}{2}\rho U^2} \leq \frac{u_0}{U} \left[\frac{9}{32} \frac{\delta_0}{a} \frac{u_0}{U} + 0.6723 \frac{\delta_0}{U} \frac{du_0}{dz} \right] \quad (2)$$

where $L \geq W$ and $W = 4\pi/3 \rho_s g a^3$.

The quantity $\rho_s g \delta_0 / \frac{1}{2}\rho U^2$ has been termed the loading parameter by Vidal and the same definition will be continued here. This definition of loading parameter is based upon the local dynamic pressure. Hence the loading parameter assumes an infinite value at stagnation point and decreases steadily outward. This parameter can be redefined in terms of maximum surface dynamic pressure ($\frac{1}{2}\rho U_m^2$), which is also equal to dynamic pressure on the free jet axis at an upstream distance, ($z = Z_\infty$) where the effect of the ground surface is negligible. This has the advantage that not only the loading parameter becomes constant with respect to radial distance,

Particle in boundary layer shear flow.

this difference is that the boundary layer was too thin (0.02-0.08 cm). As a result, only a few particles were fully immersed in the boundary layer and the majority of the particles projected well outside. Moreover, the small particles which were fully immersed and could have been normally entrained due to lift are surrounded by larger ones and hence are protected to some extent from being displaced. This in turn necessitates larger surface dynamic pressures to dislodge them, resulting in a lower loading parameter. However, in practice, the VTOL configurations are many times larger than the 40.64 cm ducted fan and hence the boundary layer thickness can be such that bulk of the terrain particles can be fully immersed in it. Hence, the present criteria can be expected to give reasonably good results.

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J80-197 Optimal Design of Ring Stiffened Cylindrical Shells Using Multiple Stiffener Sizes

Michael Pappas* and Jacob Moradi†
New Jersey Institute of Technology, Newark, N.J.

Introduction

KUNOO and Yang¹ investigated minimum weight cylindrical shells stiffened with both multiple size "I"-type rings and stringers using discrete stiffener buckling theory. They obtained a savings in weight of about 5% with the use of two ring and two stringer sizes for the example studied. Approximation methods are employed to reduce the computational effort required to approach a solution within reasonable bounds on cost (about 2000 s on a CDC 6500). Oddly, no mention is made in their work of the coalescence of buckling modes, a characteristic of optimal designs controlled by buckling behavior. Furthermore, their procedure apparently does not consider this situation.

This Note studies a "T"-type ring-stiffened shell problem by direct optimization without use of approximations or

limitations in the number of stiffener sizes like those used in Ref. 1. The optimization formulation and procedure used here admit a large number of simultaneous buckling modes, thus allowing optimization under conditions of mode coalescence.

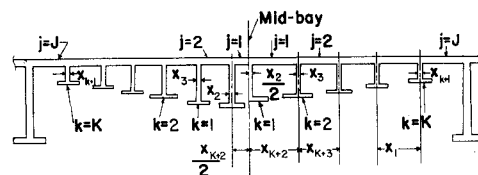
Procedure

The variables employed for this problem are skin thickness and ring dimensions and spacing. Each ring size used introduces a variable set associated with its dimensions. Thus, the number of variables is dependent on the number of sizes employed. To reduce problem dimensionality in this preliminary study, it is useful to introduce several assumptions. It is assumed that the shell is symmetrical with respect to a plane at midshell normal to the cylinder axis, that the ring flange thickness is equal to the web thickness, and that the flange width and web height are set at the maximum permitted to prevent local flange or web buckling.² It is shown in Ref. 2 that these assumptions have little effect on the optimal structural weight. The resulting problem variables as shown in Fig. 1.

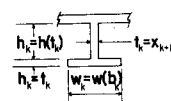
Constraints on ring and skin yielding are applied in a fashion similar to Ref. 2 except that here a separate constraint must be considered for each shell panel. To determine the buckling pressures for the range of parameters of interest in this study, one could prudently examine all mode combinations where n (the number of circumferential waves) ranges from 0 to 20 and m (the number of axial half-waves) from 1 to 40. Using the analytical procedure of Refs. 3 and 4, this would involve the solution of several hundred eigenvalue problems of rank 840 (21×40) during a single optimization run. It may be seen, however, from an examination of the equations of Ref. 3 that for the case of uniform stiffeners the buckling modes are uncoupled with respect to n and interact only with respect to even or odd m . Thus, a single 840×840 problem can be reduced to a series of forty-two 20×20 problems substantially reducing computational effort required to determine buckling behavior. Furthermore, since most constraint function evaluations are for very similar designs, computational effort may be again reduced by restricting the range of odd or even m terms included in the formulation of the eigenvalue problem for a particular n based on a knowledge of the range necessary to include all m terms making a significant contribution. Likewise, only those n values which appear to be "critical" with respect to buckling need be examined.

Thus, let v_{mn}^s be the value of an element of the matrix of eigenvectors which represents the buckling behavior of the design x^s , and m_n^s be the value of m associated with the largest value of the component v_{mn}^s of vector v_n^s . Now, using the procedure of Ref. 3 starting from $n = n_{\min}$, where n_{\min} is the lowest n considered, and setting an index $i = 1$, set up and solve an M by M eigenvalue problem P_n^s for design x^s using terms associated with

$$m = m_{\min}, m_{\min} + 2, m_{\min} + 4, \dots, m_{\max} \quad (1)$$



a) Typical cross-section showing variable designations for odd and even numbers of frames



b) Dimensions of the k-th frame

Fig. 1 Shell design variables.

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*Associate Professor, Dept. of Mechanical Engineering.

†Research Associate, Dept. of Mechanical Engineering; presently, Body Engineer, Structural Analysis Dept., Chrysler Corp., Detroit, Michigan.